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Centre number

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Candidate number

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Surname

Forename(s)

Candidate signature

I declare this is my own work.

A-level MATHEMATICS

Paper 1

Tuesday 4 June 2024

Afternoon

Time allowed: 2 hours

Materials

- You must have the AQA Formulae for A-level Mathematics booklet.
- You should have a graphical or scientific calculator that meets the requirements of the specification.

Instructions

- Use black ink or black ball-point pen. Pencil should only be used for drawing.
- Fill in the boxes at the top of this page.
- Answer **all** questions.
- You must answer each question in the space provided for that question.
- If you need extra space for your answer(s), use the lined pages at the end of this book. Write the question number against your answer(s).
- Do **not** write outside the box around each page or on blank pages.
- Show all necessary working; otherwise marks for method may be lost.
- Do all rough work in this book. Cross through any work that you do not want to be marked.

Information

- The marks for questions are shown in brackets.
- The maximum mark for this paper is 100.

Advice

- Unless stated otherwise, you may quote formulae, without proof, from the booklet.
- You do not necessarily need to use all the space provided.

For Examiner's Use	
Question	Mark
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TOTAL	



J U N 2 4 7 3 5 7 1 0 1

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Answer **all** questions in the spaces provided.

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outside the
box

- 1** Find the coefficient of x in the expansion of

$$(4x^3 - 5x^2 + 3x - 2)(x^5 + 4x + 1)$$

Circle your answer.

[1 mark]

–5

–2

7

11



2 The function f is defined by $f(x) = e^x + 1$ for $x \in \mathbb{R}$

Find an expression for $f^{-1}(x)$

Tick (✓) **one** box.

[1 mark]

$$f^{-1}(x) = \ln(x - 1)$$

☐

$$f^{-1}(x) = \ln(x) - 1$$

☐

$$f^{-1}(x) = \frac{1}{e^x + 1}$$

☐

$$f^{-1}(x) = \frac{x - 1}{e}$$

☐

Turn over for the next question

Turn over ►



3 The expression

$$\frac{12x^2 + 3x + 7}{3x - 5}$$

can be written as

$$Ax + B + \frac{C}{3x - 5}$$

State the value of A

Circle your answer.

[1 mark]

3

4

7

9

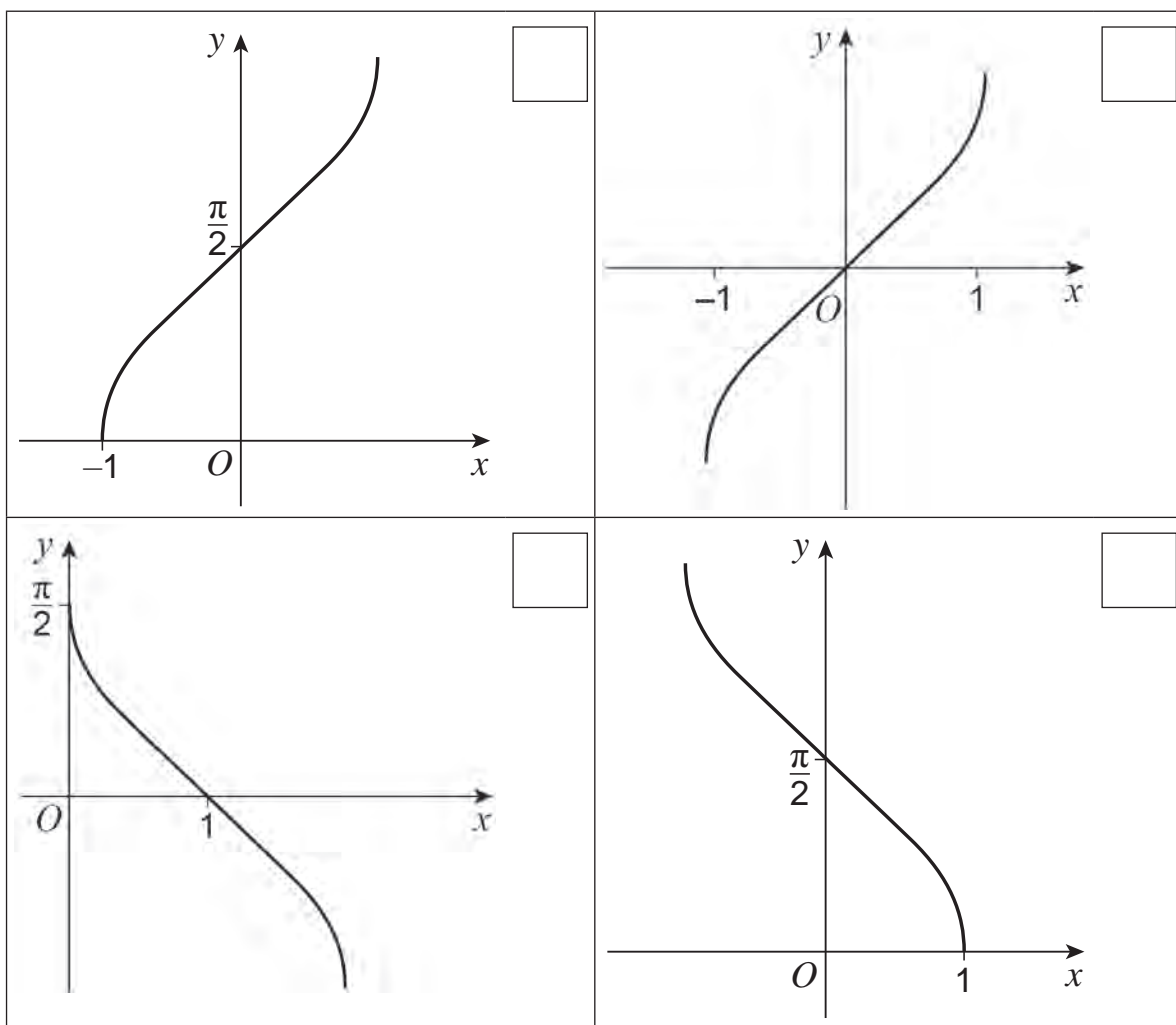


4 One of the diagrams below shows the graph of $y = \arccos x$

Identify the graph of $y = \arccos x$

Tick (✓) **one** box.

[1 mark]



Turn over for the next question

Turn over ►



6 Use the chain rule to find $\frac{dy}{dx}$ when $y = (x^3 + 5x)^7$

[2 marks]

Turn over for the next question

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- 8 (a)** Find the first three terms, in ascending powers of x , in the expansion of

$$(2 + kx)^5$$

where k is a positive constant.

[3 marks]

- 8 (b)** Hence, given that the coefficient of x is four times the coefficient of x^2 , find the value of k

[2 marks]

Turn over ►



9 (b) Use your answer to part **(a)** to find an approximation for

$$\cos 0.28 + 2 \sin 0.21 - \tan 0.14$$

Give your answer to three decimal places.

[2 marks]

Turn over for the next question

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10 (a) An arithmetic sequence has 300 terms.

The first term of the sequence is -7 and the last term is 32

Find the sum of the 300 terms.

[2 marks]



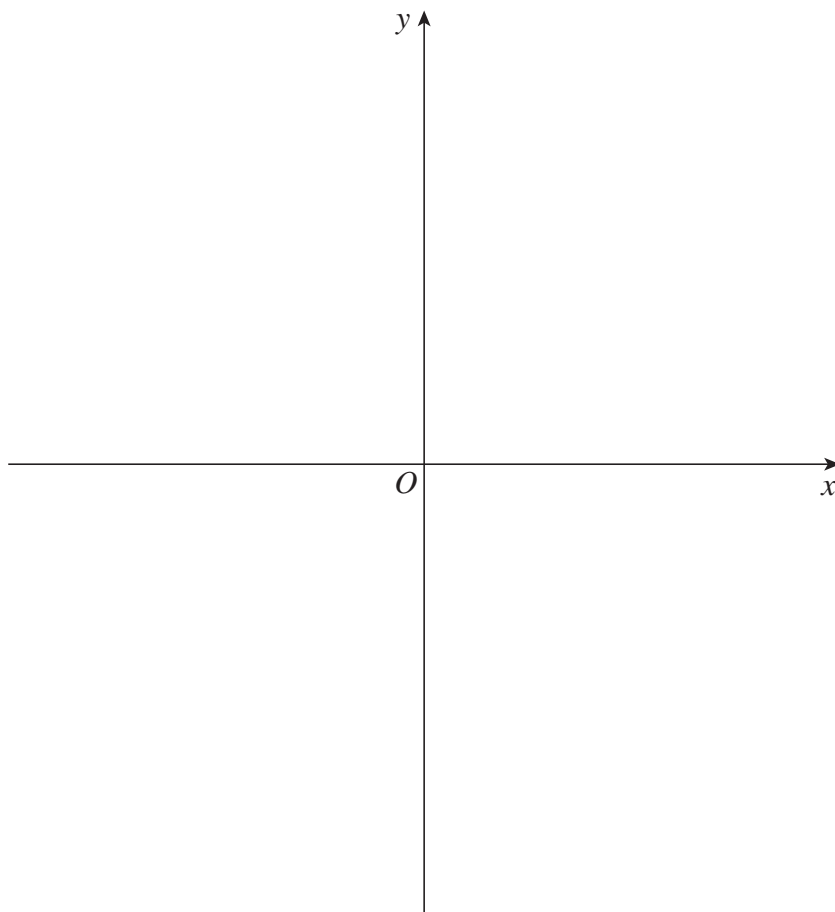
11 It is given that

$$f(x) = x(x - a)(x - 6)$$

where $0 < a < 6$

11 (a) Sketch the graph of $y = f(x)$ on the axes below.

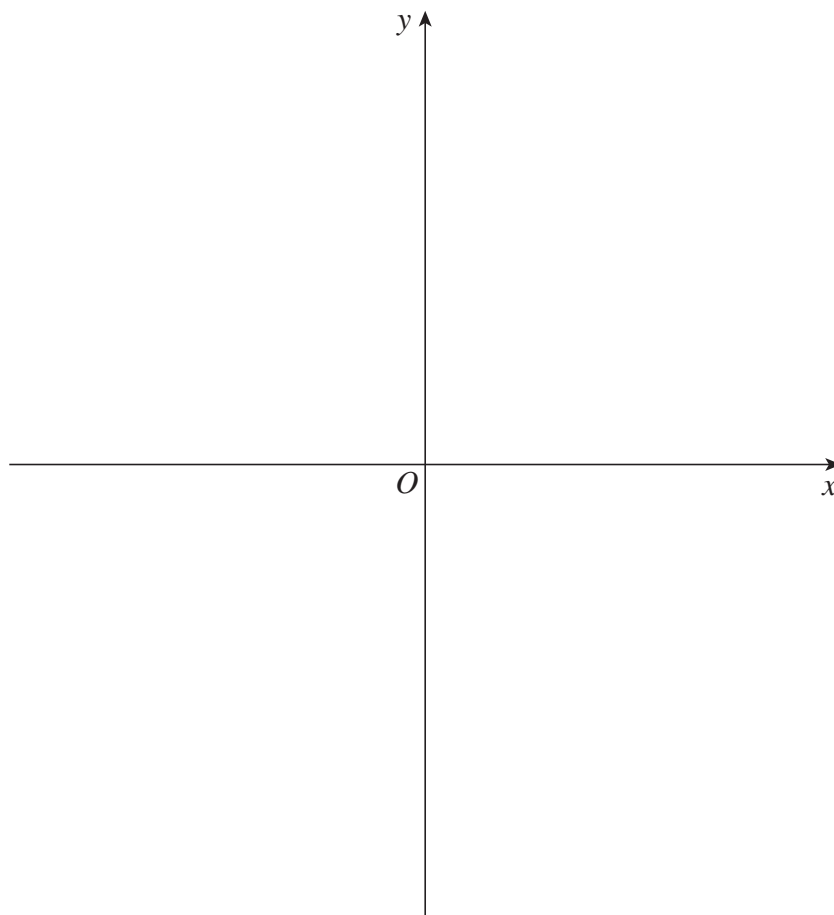
[3 marks]



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11 (b) Sketch the graph of $y = f(-2x)$ on the axes below.

[2 marks]



Turn over for the next question

Turn over ►



12 The terms, u_n , of a periodic sequence are defined by

$$u_1 = 3 \quad \text{and} \quad u_{n+1} = \frac{-6}{u_n}$$

12 (a) Find u_2 , u_3 and u_4

[2 marks]

12 (b) State the period of the sequence.

[1 mark]



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12 (c) Find the value of $\sum_{n=1}^{101} u_n$

[2 marks]

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13 (a) It is given that

$$P(x) = 4x^3 + 8x^2 + 11x + 4$$

Use the factor theorem to show that $(2x + 1)$ is a factor of $P(x)$

[2 marks]

13 (b) Express $P(x)$ in the form

$$P(x) = (2x + 1)(ax^2 + bx + c)$$

where a , b and c are constants to be found.

[2 marks]



13 (c)

Given that n is a positive integer, use your answer to part **(b)** to explain why $4n^3 + 8n^2 + 11n + 4$ is **never** prime.

[2 marks]

Turn over for the next question

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14 (a) The equation

$$x^3 = e^{6-2x}$$

has a single solution, $x = \alpha$

By considering a suitable change of sign, show that α lies between 0 and 4

[2 marks]

14 (b) Show that the equation $x^3 = e^{6-2x}$ can be rearranged to give

$$x = 3 - \frac{3}{2} \ln x$$

[3 marks]



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14 (c) (i) Use the iterative formula

$$x_{n+1} = 3 - \frac{3}{2} \ln x_n$$

with $x_1 = 4$, to find x_2 , x_3 and x_4

Give your answers to three decimal places.

[2 marks]

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14 (c) (ii) Figure 1 below shows a sketch of parts of the graphs of

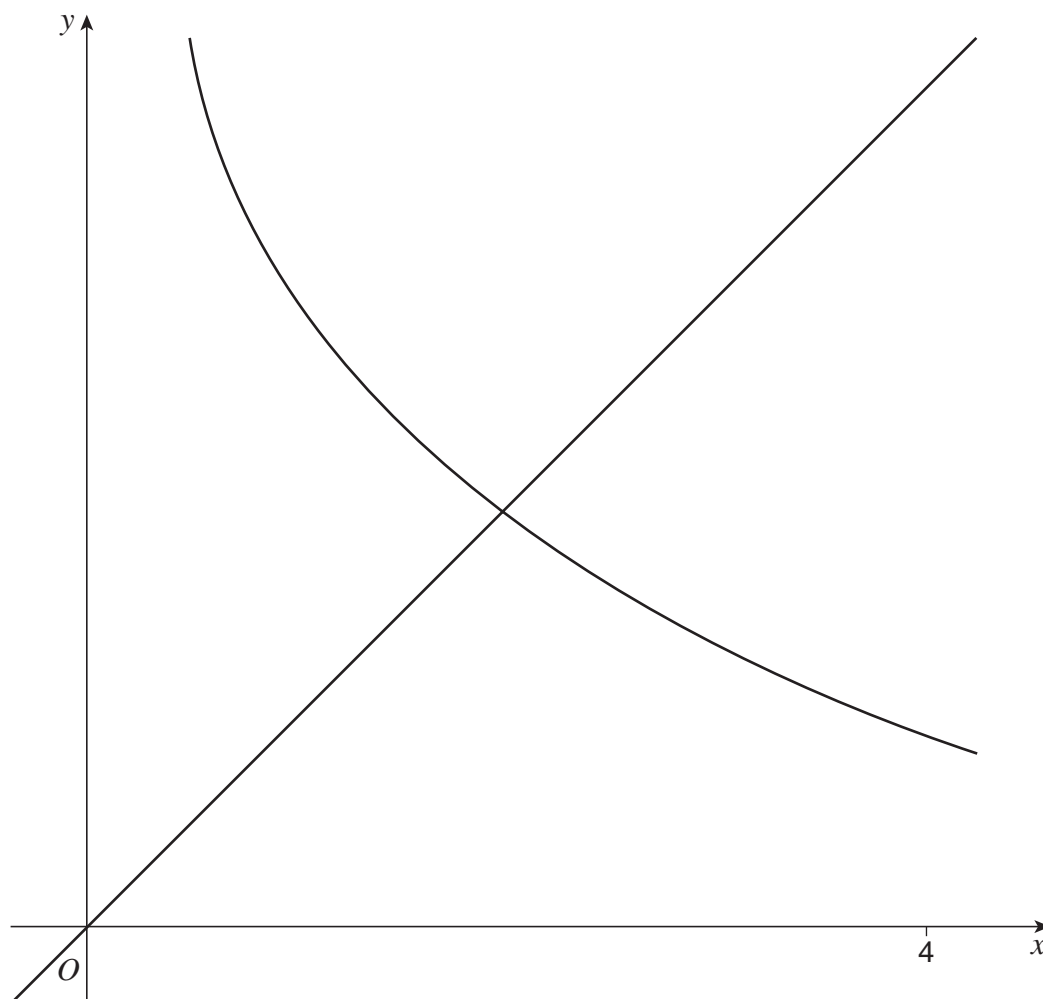
$$y = 3 - \frac{3}{2} \ln x \text{ and } y = x$$

On **Figure 1**, draw a staircase or cobweb diagram to show how convergence takes place.

Label, on the x -axis, the positions of x_2 , x_3 and x_4

[2 marks]

Figure 1



14 (c) (iii) Explain why the iterative formula

$$x_{n+1} = 3 - \frac{3}{2} \ln x_n$$

fails to converge to α when the starting value is $x_1 = 0$

[1 mark]

Turn over for the next question

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- 15 (b)** A student is attempting to solve the equation

$$\sin 2\theta \operatorname{cosec} \theta + \cos 2\theta \sec \theta = 3 \text{ for } 0^\circ \leq \theta \leq 360^\circ$$

They use the result from part (a), and write the following **incorrect** solution:

$$\sin 2\theta \operatorname{cosec} \theta + \cos 2\theta \sec \theta = 3$$

Step 1 $4 \cos \theta - \sec \theta = 3$

Step 2 $4 \cos \theta - \frac{1}{\cos \theta} - 3 = 0$

Step 3 $4 \cos^2 \theta - 3 \cos \theta - 1 = 0$

Step 4 $\cos \theta = 1$ or $\cos \theta = -0.25$

Step 5 $\theta = 0^\circ, 104.5^\circ, 255.5^\circ, 360^\circ$

- 15 (b) (i)** Explain why the student should reject one of their values for $\cos \theta$ in Step 4.

[1 mark]

- 15 (b) (ii)** State the correct solutions to the equation

$$\sin 2\theta \operatorname{cosec} \theta + \cos 2\theta \sec \theta = 3 \text{ for } 0^\circ \leq \theta \leq 360^\circ$$

[1 mark]

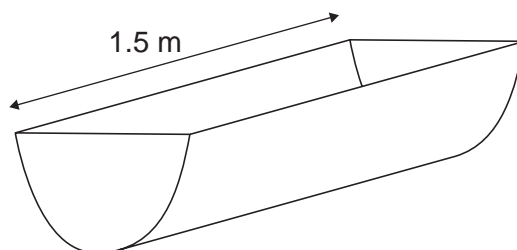
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16

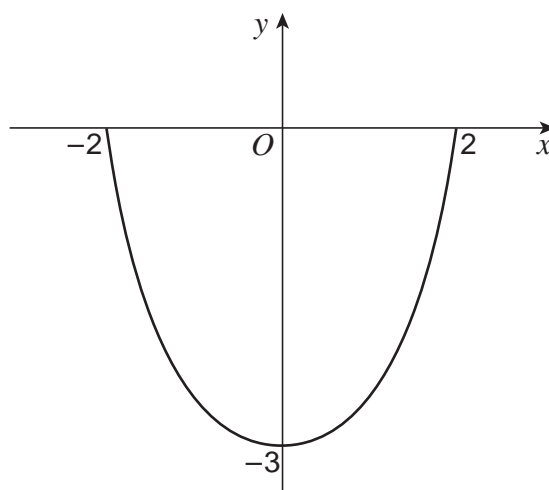
Figure 2 below shows a 1.5 metre length of pipe.

Figure 2



The symmetrical cross-section of the pipe is shown below, in **Figure 3**, where x and y are measured in centimetres.

Figure 3



17 The function f is defined by

$$f(x) = |x| + 1 \text{ for } x \in \mathbb{R}$$

The function g is defined by

$$g(x) = \ln x$$

where g has its greatest possible domain.

17 (a) Using set notation, state the range of f

[2 marks]

17 (b) State the domain of g

[1 mark]

17 (c) The composite function h is given by

$$h(x) = gf(x) \text{ for } x \in \mathbb{R}$$

17 (c) (i) Write down an expression for $h(x)$ in terms of x

[1 mark]



17 (c) (ii) Determine if h has an inverse.

Fully justify your answer.

[2 marks]

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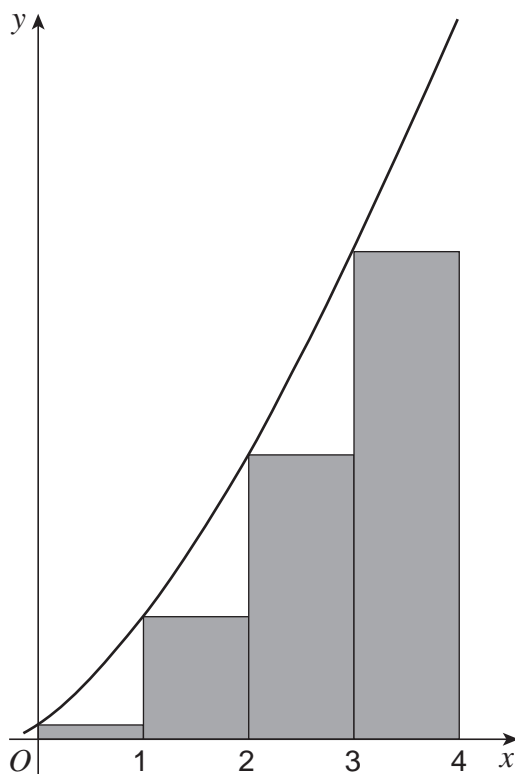
18 (c) A graph has the equation

$$y = (4x + 1)\sqrt{2x + 1}$$

A student uses four rectangles to approximate the area under the graph between the lines $x = 0$ and $x = 4$

The rectangles are all the same width.

All the rectangles are drawn under the curve as shown in the diagram below.



The total area of the four rectangles is A

The student decides to improve their approximation by increasing the number of rectangles used.

Explain why the value of the student's improved approximation will be

greater than A , but less than $\frac{1322}{15}$

[2 marks]

Turn over for the next question

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20 (b) Solve the differential equation

$$\frac{dh}{dt} = -0.012(h - 5)$$

to find an expression for h in terms of t

[5 marks]

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20 (c) Find the time taken for the container to be half empty.

Give your answer to the nearest minute.

[2 marks]

END OF QUESTIONS



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